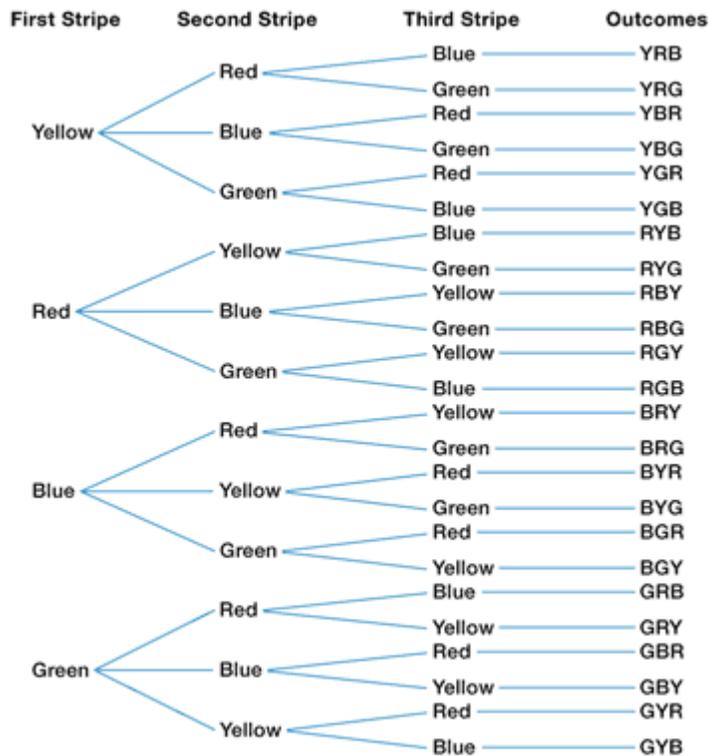


Permutations and Combinations

Example 1 Tree Diagram Permutation

Mrs. Malone assigned a project to her art class. Each student is to design a flag. The background of the flag consists of 3 wide stripes. If there are 4 colors available for the 3 stripes and each stripe must be a different color. How many possible flags are there?

Use a tree diagram to show the possible arrangements.



There are 24 different ways the students can color the background of their flags.

b. If the books are chosen randomly, what is the probability that 2 British literature, 3 contemporary literature, and 1 Western literature book will be selected?

There are three questions to consider.

- How many ways can 2 British literature books be chosen from 4?
- How many ways can 3 contemporary literature books be chosen from 5?
- How many ways can 1 Western literature book be chosen from 3?

Using the Fundamental Counting Principle, the answer can be determined with the product of the three combinations.

ways to choose 2 British literature books out of 4	ways to choose 3 contemporary literature books out of 5	ways to choose 1 Western literature book out of 3
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$${}_4C_2 \quad \cdot \quad {}_5C_3 \quad \cdot \quad {}_3C_1$$

$$\begin{aligned}
 ({}_4C_2)({}_5C_3)({}_3C_1) &= \frac{4!}{(4-2)!2!} \cdot \frac{5!}{(5-3)!3!} \cdot \frac{3!}{(3-1)!1!} && \text{Definition of combination} \\
 &= \frac{4!}{2!2!} \cdot \frac{5!}{2!3!} \cdot \frac{3!}{2!1!} && \text{Simplify.} \\
 &= \frac{4 \cdot 3}{2 \cdot 1} \cdot \frac{5 \cdot 4}{2 \cdot 1} \cdot \frac{3}{1} && \text{Divide each by the GCF.} \\
 &= \frac{720}{4} \text{ or } 180 && \text{Simplify.}
 \end{aligned}$$

Finally, there are 180 ways to choose this particular combination out of 924 possible combinations.

$$\begin{aligned}
 P(2 \text{ British, } 3 \text{ contemporary, } 1 \text{ Western}) &= \frac{180}{924} && \leftarrow \text{ number of favorable outcomes} \\
 & && \leftarrow \text{ number of possible outcomes} \\
 &= \frac{15}{77} && \text{Simplify.}
 \end{aligned}$$

The probability that the literature teacher will randomly select 2 British literature books, 3 contemporary literature books, and 1 Western literature book is $\frac{15}{77}$ or about 19%.