

# Math 8

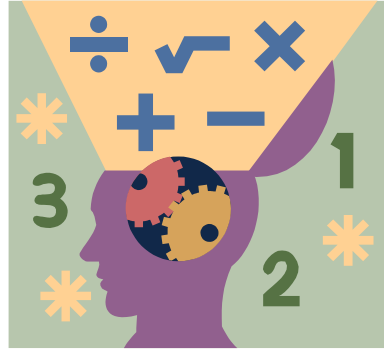


Colonial School District

## Summer Math Packet Answer key

The concepts included in this packet will help reinforce key skills your child has encountered in math this year. Please encourage them to complete as many activities as possible as it will lead to greater success next year. The answer key to this packet is available on the district website ([www.colonialsd.org](http://www.colonialsd.org)).

June 2019



Dear Parents/Guardians,

First, we would like to thank you for all of the additional support you offer at home. Education is a true partnership between school and family that is essential to a child's success.

As this school year comes to a close, we wanted to again encourage you to continue to reinforce and foster the mathematical skills and practices that have been developed this year by scheduling time for your child to work through this summer math packet. The activities were selected by our grade level experts with the key mathematical concepts of the school year in mind. The ultimate goal is to reinforce and strengthen the skills that will serve as building blocks for future learning.

Wishing you a relaxing, yet exciting, math-filled summer!

Sincerely,

The Curriculum Department

# Equations

Key

## One-step Equations

RULE	EXAMPLE
1. Look at what has been done to the variable. 2. Undo it using the inverse operation on both sides of the equation. 3. Check your answer by replacing the variable with the solution.	$\begin{array}{r} x - 15 = 29 \\ +15 \quad +15 \\ \hline x = 44 \end{array}$ $\checkmark 44 - 15 = 29$

Solve.

$$\begin{array}{r} 1. \ d + 32 = 70 \\ -32 \quad -32 \\ \hline d = 38 \end{array}$$

$$\begin{array}{r} 2. \ 708 = c + 30 \\ -30 \quad -30 \\ \hline 678 = c \end{array}$$

$$\begin{array}{r} 3. \ x - 89 = 176 \\ +89 \quad +89 \\ \hline x = 265 \end{array}$$

$$\begin{array}{r} 4. \ x - 36 = 12 \\ +36 \quad +36 \\ \hline x = 48 \end{array}$$

$$\begin{array}{r} 5. \ 5x = 225 \\ \overline{5} \quad \overline{5} \\ x = 45 \end{array}$$

$$\begin{array}{r} 6. \ 12n = 96 \\ \overline{12} \quad \overline{12} \\ n = 8 \end{array}$$

$$\begin{array}{r} 7. \ n \div 72 = 360 \\ \times 72 \quad \times 72 \\ \hline n = 25,920 \end{array}$$

$$\begin{array}{r} 8. \ n \div 12 = 12 \\ \times 12 \quad \times 12 \\ \hline n = 144 \end{array}$$

# Fractions: Solving Equations

Name

Key

Solve and check each equation.

$$n - \frac{6}{8} = \frac{2}{3}$$

$$n - \frac{6}{8} + \frac{6}{8} = \frac{2}{3} + \frac{6}{8}$$

$$n = 1\frac{5}{12}$$

$$1\frac{5}{12} - \frac{6}{8} = \frac{2}{3}$$

$$\frac{17}{12} - \frac{6}{8} = \frac{2}{3}$$

$$\frac{34}{24} - \frac{18}{24} = \frac{16}{24} = \frac{2}{3} \checkmark$$

1. Look at what has been done to the variable.
2. Undo it by using the inverse (opposite) operation on both sides of the equation.

3. Check your answer by plugging it back into the equation to see if it makes the equation true.

$$1. \quad x - \frac{2}{3} = \frac{4}{9}$$

$$+ \frac{2}{3} \quad + \frac{2}{3} = \frac{6}{9}$$

$$x = \frac{10}{9} = 1\frac{1}{9}$$

$$2. \quad x + \frac{3}{4} = \frac{8}{9}$$

$$- \frac{3}{4} \quad - \frac{3}{4} = \frac{17}{36}$$

$$x = \frac{5}{36}$$

$$3. \quad m - \frac{3}{10} = \frac{5}{8}$$

$$+ \frac{3}{10} \quad + \frac{3}{10} = \frac{25}{40} + \frac{18}{40}$$

$$m = \frac{37}{40}$$

$$4. \quad \frac{5}{4} \cdot \frac{4}{5}y = 5 \cdot \frac{5}{4}$$

$$y = \frac{25}{4} = 6\frac{1}{4}$$

$$5. \quad \frac{1}{6} \cdot 6x = \frac{4}{3} \cdot \frac{1}{6}$$

$$x = \frac{4}{18} = \frac{2}{9}$$

$$6. \quad c + \frac{3}{4} = \frac{4}{5}$$

$$- \frac{3}{4} \quad - \frac{3}{4} = \frac{16}{20} - \frac{15}{20}$$

$$c = \frac{1}{20}$$

$$7. \quad y - \frac{10}{30} = \frac{2}{5} \cdot \frac{12}{30}$$

$$+ \frac{10}{30} \quad + \frac{10}{30}$$

$$y = \frac{22}{30} = \frac{11}{15}$$

$$8. \quad x + \frac{1}{2} = \frac{7}{10}$$

$$- \frac{1}{2} \quad - \frac{1}{2} = \frac{5}{10} - \frac{5}{10}$$

$$x = \frac{2}{10} = \frac{1}{5}$$

$$9. \quad 1\frac{2}{3}x = \frac{6}{5}$$

$$\frac{3}{5} \cdot \frac{5}{3}x = \frac{6}{5} \cdot \frac{3}{5}$$

$$x = \frac{18}{25}$$

$$10. \quad 1\frac{2}{9} = 18h$$

$$\frac{11}{9} \cdot \frac{1}{18} = h$$

$$\frac{11}{162} = h$$

$$11. \quad \frac{x}{12} = 2\frac{3}{10}$$

$$x = \frac{23}{5} \cdot \frac{12}{1} = \frac{138}{5}$$

$$x = 27\frac{3}{5}$$

$$12. \quad \frac{15}{35} \cdot \frac{3}{7} = x + \frac{2}{5}$$

$$\frac{14}{35} \cdot \frac{3}{5} = x$$

$$\frac{1}{5} = x$$

$$13. \quad \frac{1}{5} + y = \frac{1}{4} \cdot \frac{5}{20}$$

$$- \frac{1}{5} \quad - \frac{1}{5} = \frac{4}{20} - \frac{4}{20}$$

$$y = \frac{1}{20}$$

$$14. \quad \frac{6}{5} \cdot \frac{5}{6}x = \frac{7}{12} \cdot \frac{4}{5}$$

$$x = \frac{7}{10}$$

$$15. \quad \frac{1}{6} \cdot 6n = \frac{3}{5} \cdot \frac{1}{6}$$

$$n = \frac{3}{30} = \frac{1}{10}$$

# Equations

Key

## Two-step Equations

RULE	EXAMPLE
1. First, undo addition or subtraction.	$3x - 2 = 13$
2. Then, undo multiplication or division.	$\begin{array}{r} +2 \quad +2 \\ 3x \quad = 15 \\ 3 \quad 3 \end{array}$
3. Check your answer by replacing the variable with the solution.	$x = 5$
	$\checkmark 3 \times 5 - 2$
	$15 - 2 = 13$

Solve.

1.  $6d - 3 = 32$

$$\begin{array}{r} +3 \quad +3 \\ 6d \quad = 35 \\ \hline 6 \quad 6 \end{array}$$

$$d = 5\frac{5}{6}$$

2.  $\frac{x}{5} + 2 = 6$

$$\begin{array}{r} -2 \quad -2 \\ x \div 5 \quad = 4 \\ \hline \cdot 5 \quad \cdot 5 \\ x \quad = 20 \end{array}$$

3.  $2y + 7 = 15$

$$\begin{array}{r} -7 \quad -7 \\ 2y \quad = 8 \\ \hline 2 \quad 2 \end{array}$$

$$y = 4$$

4.  $\frac{b}{7} - 13 = 23$

$$\begin{array}{r} +13 \quad +13 \\ 7 \cdot \frac{b}{7} \quad = 36 \cdot 7 \\ \hline b \quad = 252 \end{array}$$

5.  $-5y + 9 = 24$

$$\begin{array}{r} -9 \quad -9 \\ -5y \quad = 15 \\ \hline -5 \quad -5 \end{array}$$

$$y = -3$$

6.  $\frac{f}{8} - 3 = -27$

$$\begin{array}{r} +3 \quad +3 \\ 8 \cdot \frac{f}{8} \quad = -24 \cdot 8 \\ \hline f \quad = -192 \end{array}$$

Key

# Equations

## Equations with Variables on Both Sides

RULE	EXAMPLE
1. Eliminate the variable from one side of the equation using inverse operations. 2. Undo addition or subtraction. 3. Then, undo multiplication or division. 4. Check your answer by replacing the variable with the solution.	$  \begin{array}{r}  8x - 3 = 6x + 1 \\  -6x \quad -6x \\  \hline  2x - 3 = 1 \\  + 3 \quad + 3 \\  \hline  2x = 4 \\  \frac{2x}{2} = \frac{4}{2} \\  x = 2  \end{array}  $ $  \begin{array}{r}  \checkmark 8 \times 2 - 3 = 6 \times 2 + 1 \\  16 - 3 = 12 + 1 \\  13 = 13  \end{array}  $

Solve.

1.  $3k + 10 = 2k - 21$

$$\begin{array}{r}
 -2k \quad -2k \\
 \hline
 1k + 10 = -21 \\
 -10 \quad -10 \\
 \hline
 k = -31
 \end{array}$$

3.  $18 + 4p = 6p + 11$

$$\begin{array}{r}
 -6p \quad -6p \\
 \hline
 18 - 2p = 11 \\
 -18 \quad -18 \\
 \hline
 -2p = -7 \\
 \frac{-2p}{-2} = \frac{-7}{-2} \\
 p = 3.5
 \end{array}$$

5.  $-3p + 8 = 2p - 2$

$$\begin{array}{r}
 -2p \quad -2p \\
 \hline
 -5p + 8 = -2 \\
 -8 \quad -8 \\
 \hline
 -5p = -10 \\
 \frac{-5p}{-5} = \frac{-10}{-5} \\
 p = 2
 \end{array}$$

2.  $x - 4 = 6x - 19$

$$\begin{array}{r}
 -6x \quad -6x \\
 \hline
 -5x - 4 = -19 \\
 \downarrow +4 \quad \downarrow +4 \\
 \hline
 -5x = -15 \\
 \frac{-5x}{-5} = \frac{-15}{-5} \\
 x = 3
 \end{array}$$

4.  $11h - 14 = 7 + 14h$

$$\begin{array}{r}
 -14h \quad -14h \\
 \hline
 -3h - 14 = 7 \\
 +14 \quad +14 \\
 \hline
 -3h = 21 \\
 \frac{-3h}{-3} = \frac{21}{-3} \\
 h = -7
 \end{array}$$

6.  $-t + 10 = t + 4$

$$\begin{array}{r}
 -t \quad -t \\
 \hline
 -2t + 10 = 4 \\
 -10 \quad -10 \\
 \hline
 -2t = -6 \\
 \frac{-2t}{-2} = \frac{-6}{-2} \\
 t = 3
 \end{array}$$

### FINDING RULES FOR PATTERNS

Consider the following table of values:

$x$	0	1	2	3	4	5	6
$y$	-2	2	6	10	14	18	22

Represent the relationship of  $x$  to  $y$  by an equation.

**STRATEGY:** To figure out the rule, first study the  $y$ -values.

**STEP 1:** Find a pattern for the  $y$ -values:

-2, 2, 6, 10, 14, 18, 22...

You can see that these numbers increase by 4 from one number to the next.

So the pattern involves multiples of 4. The equation will have  $4x$  as part of it.

**STEP 2:** Find each value for  $4x$ . Multiply each  $x$ -number by 4.

Substitute these " $4x$ -numbers" for the  $x$ -numbers of Step 2 and the corresponding  $y$ -numbers.

$4x$	0	4	8	12	16	20	24
$y$	-2	2	6	10	14	18	22

Notice that each  $y$ -value is 2 less than the corresponding  $4x$ -number.

Translated into an equation this statement becomes:

**SOLUTION:**  $y = 4x - 2$

Key

1. Consider the following table of values:

x	0	1	2	3	4	5	6	+1
y	1	6	11	16	21	26	31	+5

Which equation represents the relationship of x to y?

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{5}{1}$$

- a.  $y = 6x + 1$   
 b.  $y = 5x + 1$   
 c.  $y = 5x - 1$   
 d.  $y = x + 5$

2. Consider the following table of values:

x	0	1	2	3	4	5	6	1
y	2	6	10	14	18	22	26	4

Which equation represents the relationship of x to y?

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{4}{1} = 4$$

- a.  $y = 4x + 2$   
 b.  $y = 4x - 2$   
 c.  $y = 3x + 4$   
 d.  $y = 2x + 6$

3. What rule applies to the following data?

x	0	1	2	3	4	1
y	-3	-2	-1	0	1	1

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{1}{1} = 1$$

- a.  $y = x - 3$   
 b.  $y = x + 3$   
 c.  $y = 2x - 5$   
 d.  $y = x^2 - 3$

4. Which rule applies to the following table?

x	5	4	3	2	1	0	-1	-2	-3	-1
y	13	10	7	4	1	-2	-5	-8	-11	-3

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{-3}{-1} = \frac{-3}{-1} = 3$$

- a.  $y = 8x - 1$   
 b.  $y = 6x + 1$   
 c.  $y = 3x - 2$   
 d.  $y = 2x + 3$



## THE PYTHAGOREAN THEOREM

Key

One of the most famous theorems in the history of mathematics is the **Pythagorean Theorem**. It has to do with the sides of right triangles:

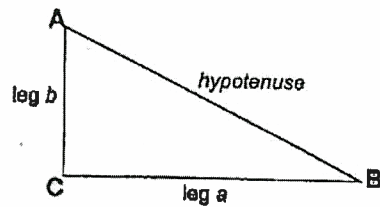
### The Pythagorean Theorem

*In any right triangle, the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the legs.*

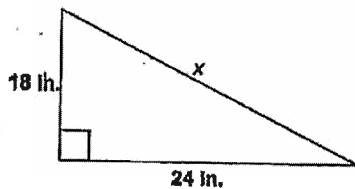
As a formula, the Pythagorean Theorem is:

$$a^2 + b^2 = c^2$$

You will often use this formula to solve problems.



1. What is  $x$ ?



- a. 12 in.
- ☒ b. 30 in.
- c. 36 in.
- d. 40 in.

$$18^2 + 24^2 = x^2$$

$$324 + 576 = x^2$$

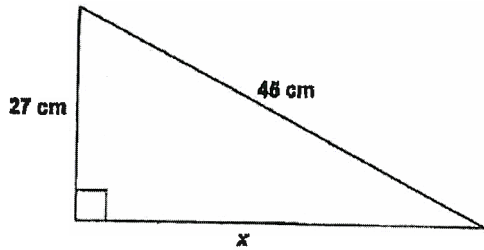
$$900 = x^2$$

$$\sqrt{900} = x$$

$$30 = x$$

Key

2. What is  $x$ ?



- a. 20 cm  
b. 25 cm  
c. 28 cm  
d. 36 cm

$$\begin{aligned} 27^2 + x^2 &= 48^2 \\ 729 + x^2 &= 2304 \\ -729 &\quad -729 \\ \hline x^2 &= 1575 \\ x &= \sqrt{1575} \\ x &= 39.7 \end{aligned}$$

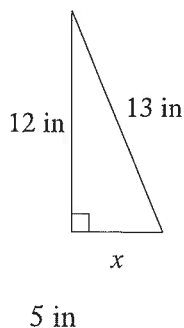
3. The length and width of a rectangle are 12 m and 5 m. What is the length of the diagonal? Show your work.

$$\begin{aligned} 12^2 + 5^2 &= x^2 \\ 144 + 25 &= x^2 \\ 169 &= x^2 \\ \sqrt{169} &= x \\ 13 \text{ m} &= x \end{aligned}$$

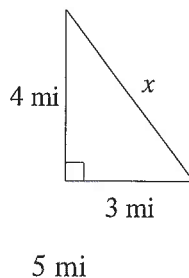
## The Pythagorean Theorem and Its Converse

Find the missing side of each triangle. Round your answers to the nearest tenth if necessary.

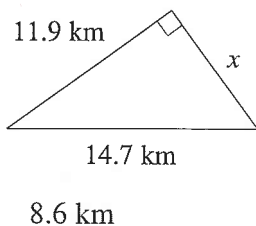
1)



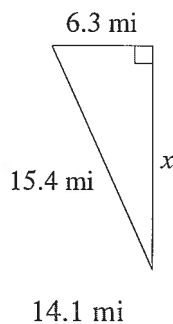
2)



3)

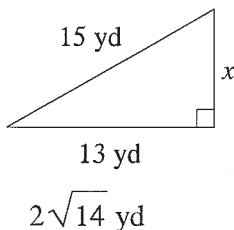


4)

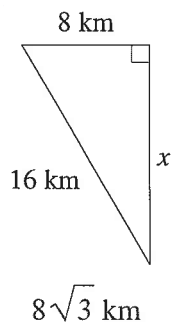


Find the missing side of each triangle. Leave your answers in simplest radical form.

5)



6)



Find the missing side of each right triangle. Side  $c$  is the hypotenuse. Sides  $a$  and  $b$  are the legs. Leave your answers in simplest radical form.

7)  $a = 11$  m,  $c = 15$  m

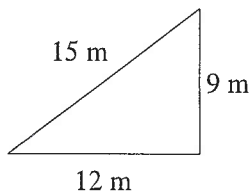
$2\sqrt{26}$  m

8)  $b = \sqrt{6}$  yd,  $c = 4$  yd

$\sqrt{10}$  yd

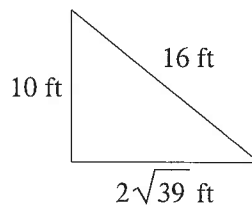
State if each triangle is a right triangle.

9)



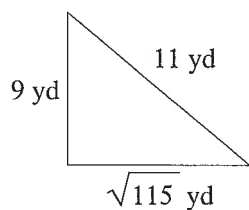
Yes

10)



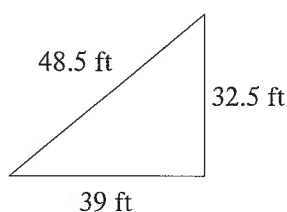
Yes

11)



No

12)



No

State if the three sides lengths form a right triangle.

13) 10 cm, 49.5 cm, 50.5 cm

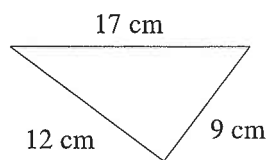
Yes

14) 9 in, 12 in, 15 in

Yes

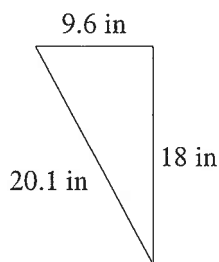
State if each triangle is acute, obtuse, or right.

15)



Obtuse

16)



Acute

State if the three side lengths form an acute, obtuse, or right triangle.

17) 6 mi,  $2\sqrt{55}$  mi, 17 mi

Obtuse

18) 4.8 km, 28.6 km, 29 km

Right

Name

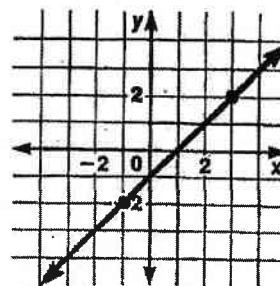
Key

Date

# Reteaching Worksheet 8-6

## Graphing Equations

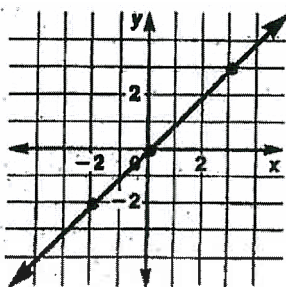
An equation has many ordered pairs of values that are solutions. For example, four ordered pairs for the equation  $y = x - 1$  are  $(3, 2)$ ,  $(0, -1)$ ,  $(2, 1)$ , and  $(-1, -2)$ . There are too many to name so a picture is drawn of them. This picture is called a graph of the equation. The graph of  $y = x - 1$  is the line drawn on the coordinate system at the right.



Find three ordered pairs that satisfy each equation. Graph each ordered pair. Draw a line through the points.

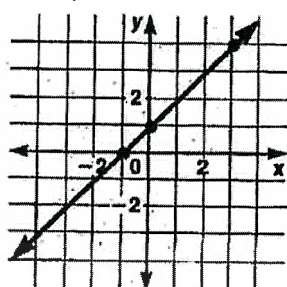
1.  $y = x$

x	y
-2	-2
0	0
3	3



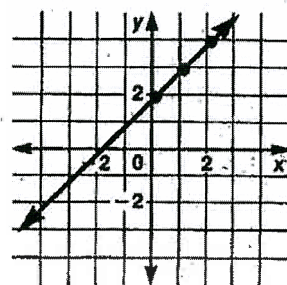
2.  $y = x + 1$

x	y
-1	0
0	1
3	4



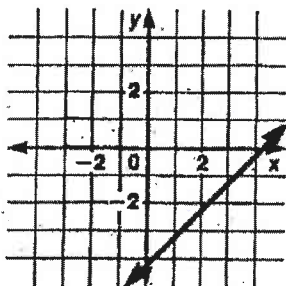
3.  $y = x + 2$

x	y
0	2
1	3
2	4

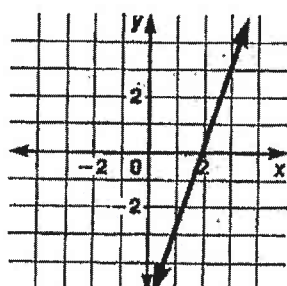


Graph each equation.

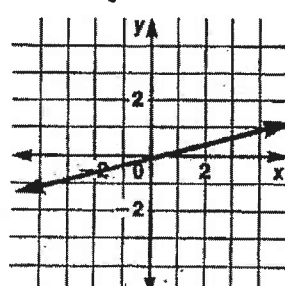
4.  $y = x - 4$



5.  $y = 3x + (-5)$



6.  $y = \frac{1}{4}x$



**EXTRA PRACTICE 29**  
Slope and Equations of Lines  
Use after Section 7.2

Name Key

Examples:

- a) Find a slope-intercept equation for the line with slope 2 that contains (0,5).

$$y = mx + b$$

The slope-intercept equation.

$$y = 2x + 5$$

Substitute 2 for  $m$  and 5 for  $b$ .

- b) Find an equation of a line that contains the points (5,-2) and (-2,1).

$$m = \frac{1 - (-2)}{-2 - 5} = \frac{3}{-7} = -\frac{3}{7}$$

First find the slope.

$$y = -\frac{3}{7}x + b$$

Using the slope-intercept form  $y = mx + b$  and substituting for  $m$ .

$$1 = -\frac{3}{7}(-2) + b$$

Using the point (-2,1) and substituting  $x = -2$  and  $y = 1$ .

(We could have just as easily used the point (5,-2)).

$$1 = \frac{6}{7} + b$$

$$\frac{1}{7} = b$$

$$y = -\frac{3}{7}x + \frac{1}{7}$$

Substitute  $b$  into  $y = mx + b$ .

$$\begin{aligned} 1. \quad -3 &= -1(4) + b \\ -3 &= -4 + b \\ 1 &= b \end{aligned}$$

$$\begin{aligned} 2. \quad 2 &= 3(-7) + b \\ 2 &= -21 + b \\ 23 &= b \end{aligned}$$

$$\begin{aligned} 5. \quad -2 &= -3(6) + b \\ -2 &= -18 + b \\ 16 &= b \end{aligned}$$

$$\begin{aligned} 7. \quad 0 &= 4(7) + b \\ 0 &= 28 + b \\ -28 &= b \end{aligned}$$

$$\begin{aligned} 9. \quad -1 &= \frac{1}{5}(5) + b \\ -1 &= 1 + b \\ -2 &= b \end{aligned}$$

Find an equation of the line containing the given point and having the given slope.

$$1. \quad (4, -3), m = -1 \quad y = -x + 1$$

$$2. \quad (-5, -6), m = 2 \quad y = 2x + 4$$

$$3. \quad (-7, 2), m = 3 \quad y = 3x + 23$$

$$4. \quad (3, 5), m = -2 \quad y = -2x + 11$$

$$5. \quad (6, -2), m = -3 \quad y = -3x + 16$$

$$6. \quad (5, -2), m = 2 \quad y = 2x - 12$$

$$7. \quad (7, 0), m = 4 \quad y = 4x - 28$$

$$8. \quad (0, 9), m = -2 \quad y = -2x + 9$$

$$9. \quad (5, -1), m = \frac{1}{5} \quad y = \frac{1}{5}x - 2$$

$$10. \quad (-3, -2), m = \frac{1}{4} \quad y = \frac{1}{4}x - \frac{1}{4}$$

$$\begin{aligned} 2. \quad -6 &= 2(-5) + b \\ -6 &= -10 + b \\ 4 &= b \end{aligned}$$

$$\begin{aligned} 4. \quad 5 &= -2(3) + b \\ 5 &= -6 + b \\ 11 &= b \end{aligned}$$

$$\begin{aligned} 6. \quad -2 &= 2(5) + b \\ -2 &= 10 + b \\ -12 &= b \end{aligned}$$

$$\begin{aligned} 8. \quad 9 &= -2(0) + b \\ 9 &= 0 + b \\ 9 &= b \end{aligned}$$

$$\begin{aligned} 10. \quad -2 &= \frac{1}{4}(-3) + b \\ -2 &= -\frac{3}{4} + b \\ -1\frac{1}{4} &= b \end{aligned}$$

Key

**EXTRA PRACTICE 29 (continued)**  
**Slope and Equations of Lines**  
 Use after Section 7.2

Find an equation of the line that contains the given pair of points

11. (1,5) and (4,2)  $y = -1x + 6$   
 $m = \frac{5-2}{1-4} = \frac{3}{-3} = -1$   
 $5 = -1(1) + b$   
 $5 = -1 + b$   
 $6 = b$

12. (-4,2) and (1,-3)  $y = -1x - 2$   
 $m = \frac{2-(-3)}{-4-1} = \frac{5}{-5} = -1$   
 $2 = -1(-4) + b$   
 $2 = 4 + b$   
 $-2 = b$

13. (-5,-3) and (1,-1)  $y = \frac{1}{3}x - \frac{1}{3}$   
 $m = \frac{-3-(-1)}{-5-1} = \frac{-2}{-6} = \frac{1}{3}$   
 $-3 = \frac{1}{3}(-5) + b$   
 $-3 = -\frac{5}{3} + b$   
 $-\frac{1}{3} = b$

14. (0,3) and (-2,6)  $y = -\frac{1}{2}x + 3$   
 $m = \frac{3-6}{0-(-2)} = \frac{-3}{2}$   
 $3 = -\frac{1}{2}(0) + b$   
 $3 = b$

15. (-8,3) and (-4,1)  $y = -\frac{1}{2}x - 1$   
 $m = \frac{3-1}{-8-(-4)} = \frac{2}{-4} = -\frac{1}{2}$   
 $3 = -\frac{1}{2}(-8) + b$   
 $3 = 4 + b$   
 $-1 = b$

16. (6,2) and (-3,0)  $y = \frac{2}{9}x + \frac{2}{3}$   
 $m = \frac{2-0}{6-(-3)} = \frac{2}{9}$   
 $2 = \frac{2}{9}(6) + b$   
 $2 = \frac{4}{3} + b$   
 $\frac{2}{3} = b$

17. (1,3) and (4,6)  $y = 1x + 2$   
 $m = \frac{3-6}{1-4} = \frac{-3}{-3} = 1$   
 $3 = 1(1) + b$   
 $3 = 1 + b$   
 $2 = b$

18. (3,-4) and (-3,4)  $y = -\frac{4}{3}x$   
 $m = \frac{-4-4}{3-(-3)} = \frac{-8}{6} = -\frac{4}{3}$   
 $-4 = -\frac{4}{3}(3) + b$   
 $-4 = -4 + b$   
 $0 = b$

19. (-7,4) and (-4,7)  $y = 1x + 11$   
 $m = \frac{4-7}{-7-(-4)} = \frac{-3}{-3} = 1$   
 $4 = 1(-7) + b$   
 $4 = -7 + b$   
 $11 = b$

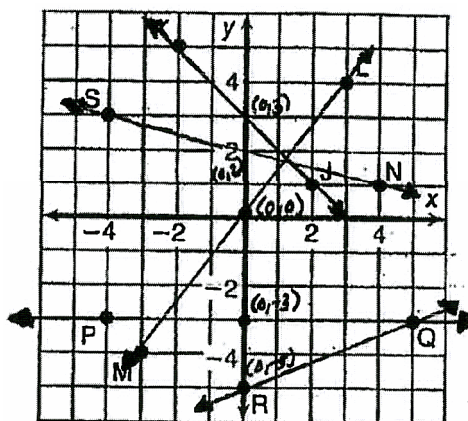
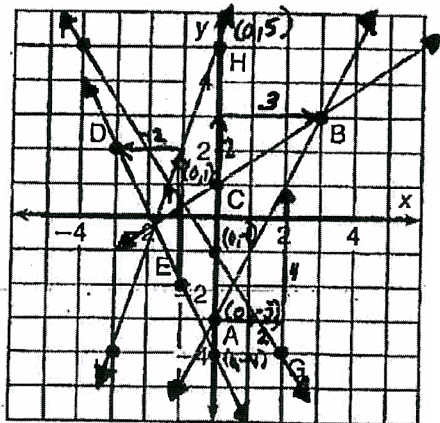
20. (9,-5) and (7,7)  $y = -6x + 49$   
 $m = \frac{-5-7}{9-7} = \frac{-12}{2} = -6$   
 $-5 = -6(9) + b$   
 $-5 = -54 + b$   
 $49 = b$



Key

# What Did the Ape Think of the Grape's House?

For each exercise, draw the line indicated and write its equation. Find your answer in the answer section and notice the two letters next to it. Print these letters in the two boxes at the bottom of the page that contain the number of that exercise.



$m = \frac{\text{rise}}{\text{run}}$

- $m = \frac{6}{3}$  ① Equation of  $\overleftrightarrow{AB}$   $y = 2x - 3$   
 $m = \frac{2}{3}$  ② Equation of  $\overleftrightarrow{CB}$   $y = \frac{2}{3}x + 1$   
 $m = -\frac{4}{2}$  ③ Equation of  $\overleftrightarrow{DE}$   $y = -2x - 4$   
 $m = -\frac{2}{1}$  ④ Equation of  $\overleftrightarrow{FG}$   $y = -\frac{3}{2}x - 1$   
 $m = \frac{2}{3}$  ⑤ Equation of  $\overleftrightarrow{HI}$   $y = 3x + 5$

- ⑥ Equation of  $\overleftrightarrow{JK}$   $y = -x + 3$   $m = -\frac{1}{4}$   
 ⑦ Equation of  $\overleftrightarrow{LM}$   $y = \frac{4}{3}x + 0$   $m = \frac{8}{6}$   
 ⑧ Equation of  $\overleftrightarrow{NS}$   $y = -\frac{1}{4}x + 2$   $m = -\frac{1}{8}$   
 ⑨ Equation of  $\overleftrightarrow{PQ}$   $y = -3$   $m = 0$   
 ⑩ Equation of  $\overleftrightarrow{RO}$   $y = \frac{2}{5}x - 5$   $m = \frac{2}{5}$

Answers:

- ~~DE~~  $y = -\frac{1}{4}x + 2$  ~~TT~~  $y = \frac{2}{5}x$  ~~EA~~  $y = -2x + 3$   
~~SA~~  $y = \frac{4}{3}x - 1$  ~~NE~~  $y = \frac{2}{3}x + 1$  ~~VI~~  $y = \frac{2}{5}x - 5$   
~~TH~~  $y = -\frac{3}{2}x + 2$  ~~OU~~  $y = -x + 3$  ~~TH~~  $y = -2x - 4$   
~~AS~~  $y = 2x - 3$  ~~GH~~  $y = -\frac{3}{2}x - 1$  ~~TI~~  $y = \frac{4}{3}x$   
~~HE~~  $y = 3x + 5$  ~~TW~~  $y = -3$  ~~SH~~  $y = \frac{2}{3}x + 5$

5	5	3	3	6	6	4	4	7	7	9	9	1	1	8	8	10	10	2	2
H	E	T	H	O	L	G	H	T	I	T	W	A	S	D	E	V	I	N	E



KEY

Practice Problems – Simplify Expressions with Exponents

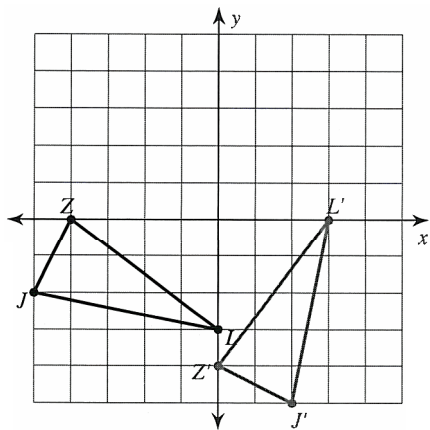
$3 \cdot 3^3$ $3^4 = 81$	$x^2 x^5$ $x^7$	$4b^2 \cdot 3b^6$ $12b^8$
$\frac{3^7}{3^2}$ $3^5$	$\frac{x^9}{x^3}$ $x^6$	$\frac{16x^8 y^5}{8x^2}$ $2x^6 y^5$
$(4^2)^3$ $4^6 = 4096$	$(x^4)^2$ $x^8$	$(y^5)^0$ $1$
$(2x^4)^2$ $2^2(x^4)^2 = 4x^8$	$(3x^5 y^3 z^4)^2$ $3^2(x^5)^2(y^3)^2(z^4)^2$ $9x^{10} y^6 z^8$	$(-2x^4 y^7 z^2)^5$ $(-2)^5(x^4)^5(y^7)^5(z^2)^5$ $-32x^{20} y^{35} z^{10}$
$\left(\frac{x^2}{3^2}\right)^2$ $\left(\frac{x^2}{3^2}\right)^2 = \frac{x^4}{9}$	$\left(\frac{x^5 y}{2z^3 y}\right)^4$ $\left(\frac{(x^5)^4}{2^4(z^3)^4}\right) = \frac{x^{20}}{16z^{12}}$	$\left(\frac{16x^8 y^7}{4x^8 y^2}\right)^4$ $(4y^5)^4 = 4^4(y^5)^4 = 256y^{20}$
$(3)^{-4}$ $\frac{1}{3^4} = \frac{1}{81}$	$\left(\frac{x}{4}\right)^{-2}$ $\left(\frac{4}{x}\right)^2 = \frac{4^2}{x^2} = \frac{16}{x^2}$	$\left(\frac{3x^2 y}{2x^3}\right)^{-4}$ $\left(\frac{2x^3}{3x^2 y}\right)^4 = \left(\frac{2x}{3y}\right)^4 = \left(\frac{2^4 x^4}{3^4 y^4}\right)$ $= \frac{16x^4}{81y^4}$

## All Transformations

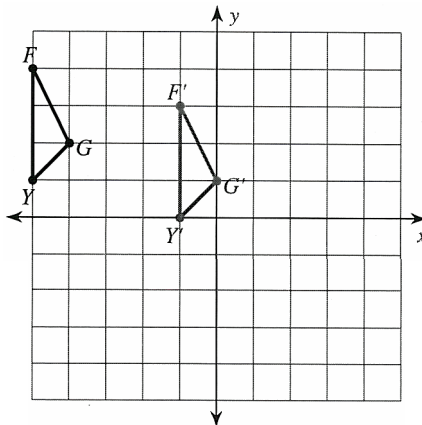
Date \_\_\_\_\_ Period \_\_\_\_\_

Graph the image of the figure using the transformation given.

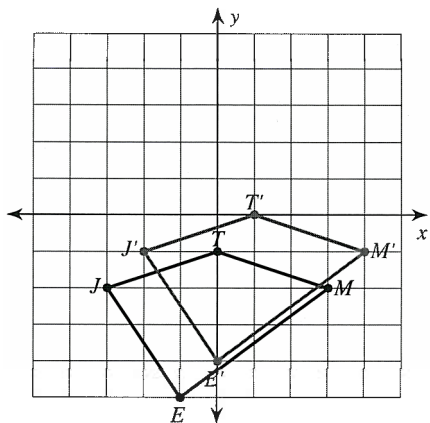
- 1) rotation
- $90^\circ$
- counterclockwise about the origin



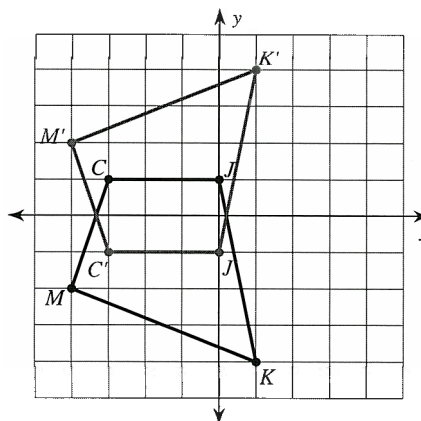
- 2) translation: 4 units right and 1 unit down



- 3) translation: 1 unit right and 1 unit up

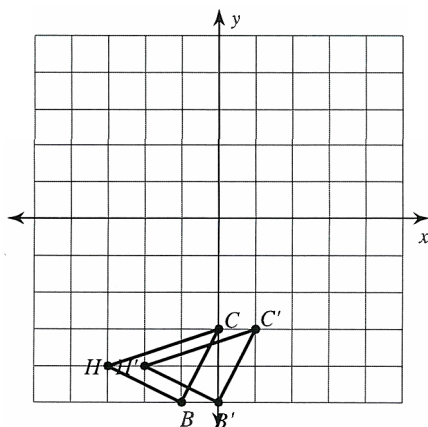


- 4) reflection across the x-axis



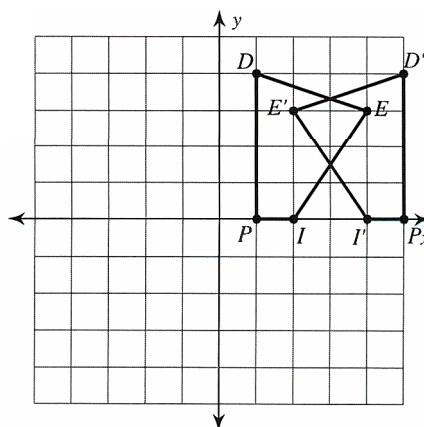
Write a rule to describe each transformation.

- 5)

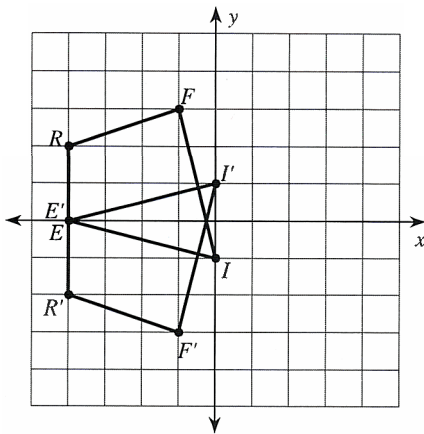


translation: 1 unit right

- 6)

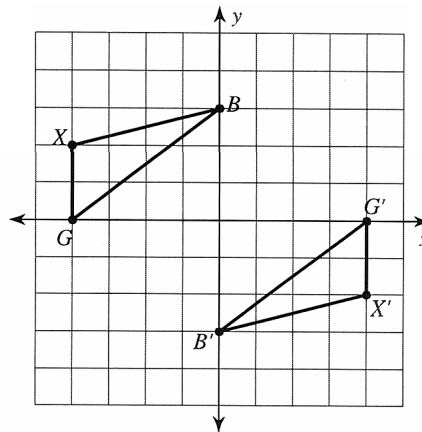
reflection across  $x = 3$

7)



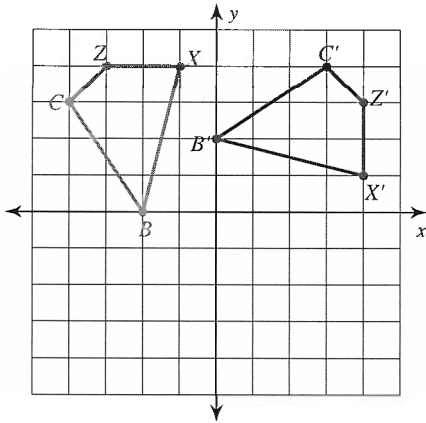
reflection across the x-axis

8)

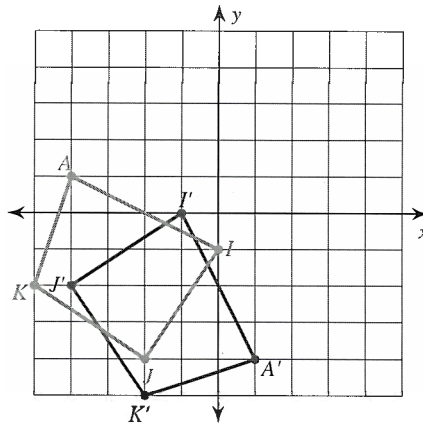
rotation  $180^\circ$  about the origin

**Graph the image of the figure using the transformation given.**

- 9) rotation  $90^\circ$  clockwise about the origin  
 $B(-2, 0)$ ,  $C(-4, 3)$ ,  $Z(-3, 4)$ ,  $X(-1, 4)$



- 10) reflection across  $y = x$   
 $K(-5, -2)$ ,  $A(-4, 1)$ ,  $I(0, -1)$ ,  $J(-2, -4)$



**Find the coordinates of the vertices of each figure after the given transformation.**

- 11) rotation  $180^\circ$  about the origin  
 $E(2, -2)$ ,  $J(1, 2)$ ,  $R(3, 3)$ ,  $S(5, 2)$   
 $E'(-2, 2)$ ,  $J'(-1, -2)$ ,  $R'(-3, -3)$ ,  $S'(-5, -2)$
- 12) reflection across  $y = 2$   
 $J(1, 3)$ ,  $U(0, 5)$ ,  $R(1, 5)$ ,  $C(3, 2)$   
 $U'(0, -1)$ ,  $R'(1, -1)$ ,  $C'(3, 2)$ ,  $J'(1, 1)$
- 13) translation: 7 units right and 1 unit down  
 $J(-3, 1)$ ,  $F(-2, 3)$ ,  $N(-2, 0)$   
 $J'(4, 0)$ ,  $F'(5, 2)$ ,  $N'(5, -1)$
- 14) translation: 6 units right and 3 units down  
 $S(-3, 3)$ ,  $C(-1, 4)$ ,  $W(-2, -1)$   
 $S'(3, 0)$ ,  $C'(5, 1)$ ,  $W'(4, -4)$

## Multiplying Binomials

Find each product.

1)  $(3n + 2)(n + 3)$

$$3n^2 + 11n + 6$$

2)  $(n - 1)(2n - 2)$

$$2n^2 - 4n + 2$$

3)  $(2x + 3)(2x - 3)$

$$4x^2 - 9$$

4)  $(r + 1)(r - 3)$

$$r^2 - 2r - 3$$

5)  $(2n + 3)(2n + 1)$

$$4n^2 + 8n + 3$$

6)  $(3p - 3)(p - 1)$

$$3p^2 - 6p + 3$$

7)  $(3p + 3)(3p + 2)$

$$9p^2 + 15p + 6$$

8)  $(k - 2)(k - 3)$

$$k^2 - 5k + 6$$

9)  $(v - 1)(3v - 3)$

$$3v^2 - 6v + 3$$

10)  $(2x - 3)(3x + 3)$

$$6x^2 - 3x - 9$$

11)  $(4n + 4)(5n - 8)$

$$20n^2 - 12n - 32$$

12)  $(5x - 2)(5x - 8)$

$$25x^2 - 50x + 16$$

13)  $(6x + 2)(2x + 8)$

$$12x^2 + 52x + 16$$

14)  $(3x + 3)(x + 4)$

$$3x^2 + 15x + 12$$

15)  $(5v + 4)(3v - 6)$

$$15v^2 - 18v - 24$$

16)  $(x - 4)(x - 7)$

$$x^2 - 11x + 28$$

17)  $(5x + 6)(8x - 4)$

$$40x^2 + 28x - 24$$

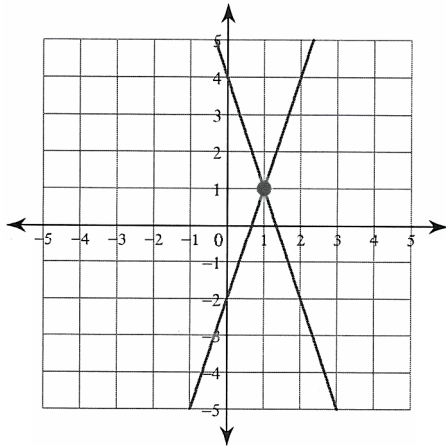
18)  $(8b - 1)(5b - 5)$

$$40b^2 - 45b + 5$$

## Systems of Two Equations

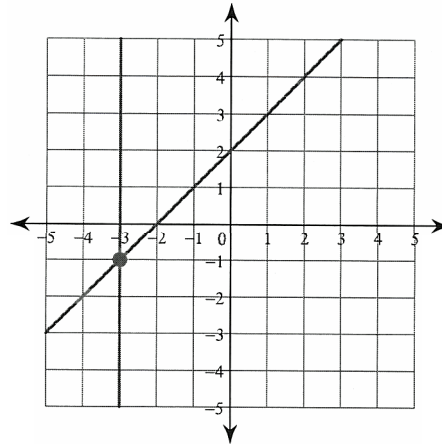
Solve each system by graphing.

$$\begin{aligned} 1) \quad y &= -3x + 4 \\ y &= 3x - 2 \end{aligned}$$



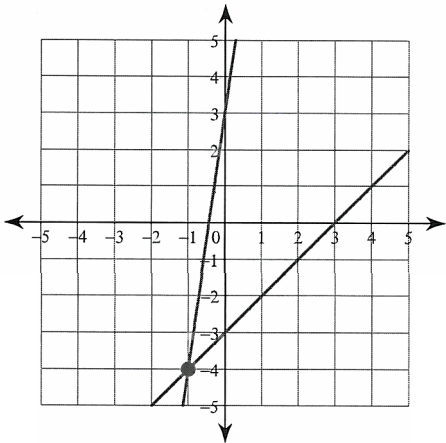
(1, 1)

$$\begin{aligned} 2) \quad y &= x + 2 \\ x &= -3 \end{aligned}$$



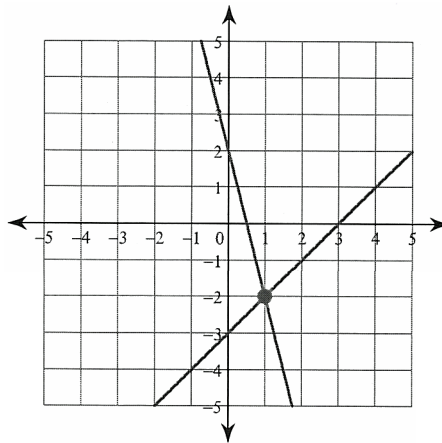
(-3, -1)

$$\begin{aligned} 3) \quad x - y &= 3 \\ 7x - y &= -3 \end{aligned}$$



(-1, -4)

$$\begin{aligned} 4) \quad 4x + y &= 2 \\ x - y &= 3 \end{aligned}$$



(1, -2)

Solve each system by substitution.

$$\begin{aligned} 5) \quad y &= 4x - 9 \\ y &= x - 3 \end{aligned}$$

(2, -1)

$$\begin{aligned} 6) \quad 4x + 2y &= 10 \\ x - y &= 13 \end{aligned}$$

(6, -7)

$$\begin{aligned} 7) \quad y &= -5 \\ 5x + 4y &= -20 \end{aligned}$$

(0, -5)

$$\begin{aligned} 8) \quad x + 7y &= 0 \\ 2x - 8y &= 22 \end{aligned}$$

(7, -1)

9)  $6x + 8y = -22$

$y = -5$

$(3, -5)$

11)  $7x + 2y = -19$

$-x + 2y = 21$

$(-5, 8)$

13)  $-7x + 4y = 24$

$4x - 4y = 0$

$(-8, -8)$

**Solve each system by elimination.**

15)  $8x - 6y = -20$

$-16x + 7y = 30$

$(-1, 2)$

17)  $-8x - 10y = 24$

$6x + 5y = 2$

$(7, -8)$

19)  $-4y - 11x = 36$

$20 = -10x - 10y$

$(-4, 2)$

21)  $0 = -2y + 10 - 6x$

$14 - 22y = 18x$

$(2, -1)$

23)  $-16 + 20x - 8y = 0$

$36 = -18y - 22x$

$(0, -2)$

10)  $-7x + 2y = 18$

$6x + 6y = 0$

$(-2, 2)$

12)  $3x - 5y = 17$

$y = -7$

$(-6, -7)$

14)  $4x - y = 20$

$-2x - 2y = 10$

$(3, -8)$

16)  $6x - 12y = 24$

$-x - 6y = 4$

$(2, -1)$

18)  $-24 - 8x = 12y$

$1 + \frac{5}{9}y = -\frac{7}{18}x$

$(6, -6)$

20)  $-9 + 5y = -4x$

$-11x = -20 + 9y$

$(1, 1)$

22)  $-16y = 22 + 6x$

$-11y - 4x = 15$

$(-1, -1)$

24)  $-\frac{5}{7} - \frac{11}{7}x = -y$

$2y = 7 + 5x$

$(-3, -4)$

**Critical thinking questions:**

25) Write a system of equations with the solution  $(4, -3)$ .

Many answers. Ex:  $x + y = 1$ ,  $2x + y = 5$

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